

# Computer Algebra (2012)-Aalborg University

## Second set of exercises

**The deadline for this set of exercises is Thursday 8/11.** I would like to get (by email) an electronic file with your solutions. Furthermore, a (brief) reasoned explanation should follow the solution of the exercises, you can write your explanation in the electronic file or print the computer solution and hand-write your explanation.

Solve the following exercises using a Computer Algebra System:

### Exercise 1

- Write a table/list with all the elements of  $\mathbb{F}_{32}$  in Maple where you consider the representation using a power of a primitive element and the polynomial notation.
- Write a table/list with all the elements of  $\mathbb{F}_{32}$  in Sage where you consider the representation using a power of a primitive element and the polynomial notation.

**Exercise 2** Which elements of  $\mathbb{F}_3/\langle X^3 + X + 1 \rangle$  are units and compute their inverse?, solve it using Sage.

**Exercise 3** Implement Algorithm 8.1 (Karatsuba) in Maple or Sage. Compute an example.

**Exercise 4** Solve Exercise 8.10 in [GG]. For “ $V_1\alpha, V_1\beta$ ” read “ $V_1f, V_1g$ ”, where  $f, g \in F^8$  are the coefficients of the polynomials  $f$  and  $g$ .

**Exercise 5** Compute the distinct-degree decomposition of the polynomial  $f$  in exercise 14.3 in [GG] using a command in Maple or Sage.

**Exercise 6** Solve Exercise 14.3 in [GG] using Maple or Sage. You do not have to implement Algorithm 14.3, but you are welcome to do it.

**Exercise 7** Factor the polynomial  $f$  in exercise 14.12 in [GG] using a command in Maple or Sage.

**Exercise 8** Solve Exercise 14.12 in [GG] using Maple or Sage. You do not have to implement Algorithm 14.10, but you are welcome to do it.

Best regards,

Diego