

# **Algebra 2 (2014)-Aalborg Universitet**

## **Spiseseddel 6**

**6. gang (B)**, fredag d. 19. februar, 8:15-12:00 i lokale G5-112

- 8:15-10:00 Forelsning: Repetition + Lecture: Euclidean domains. Fermat's two-square theorem (sider 130–134).
- 10:00-12:00 Beviser og opgaveregning:

Beviser: Proposition 3.3.2, Proposition 3.3.7, Theorem 3.3.9, Proposition 3.4.1, Corollary 3.4.2, Proposition 3.5.2, Proposition 3.5.3, Lemma 3.5.5, Proposition 3.5.6, Theorem 3.5.7, Proposition 3.5.9, Proposition 3.5.11, Theorem 3.5.15

Opgaveregning [Lau], 3.6 (side 138): 28, A, 29, 24, B, 23, C, D, 16, 13, 15, 8 (i and ii), 9 , 10, 26, 24.

Exercise A: Prove that  $\mathbb{Z}[i]$  is a Euclidean domain (see pages 132 and 133).

Exercise B: Let  $R$  be an integral domain. Prove that for  $a, b \in R$ :  $ab \in R^*$  if and only if  $a, b \in R^*$ .

Exercise C: Check that the relation defined in page 123 is an equivalent relation and the two operations are well defined.

Exercise D: Let  $R$  be a ring. Prove that  $R$  is a field if and only if  $\langle 0 \rangle$  is a maximal ideal.

Med venlig hilsen,

Diego