

Algebra 2 (2012)-Aalborg University

Lecture 5, February 19th

5th Lecture (B): Tuesday February 19th, 8:15-12:00 at room G5-112.

- 8:15-10:00 Repetition from last lecture (pages 123–126). Lecture: Unique factorization, Irreducible elements, Prime elements (126–130).
- 10:00-12:00 Work in groups: proofs + exercises.

Proofs: Proposition 3.3.2, Proposition 3.3.7, Theorem 3.3.9, Proposition 3.4.1, Corollary 3.4.2, Proposition 3.5.2, Proposition 3.5.3, Lemma 3.5.5, Proposition 3.5.6, Theorem 3.5.7.

Exercises from [Lau], 3.6 (page 138): 24, A, 23, B, C, 16, 13, 15, 8 (i and ii), 9, 10, 26, 24.

Exercise A: Let R be an integral domain. Prove that for $a, b \in R$: $ab \in R^*$ if and only if $a, b \in R^*$.

Exercise B: Check that the relation defined in page 123 is an equivalent relation and the two operations are well defined.

Exercise C: Let R be a ring. Prove that R is a field if and only if $\langle 0 \rangle$ is a maximal ideal.

Best regards,

Diego